

Turbulent Premixed Combustion

CEFRC Combustion Summer School

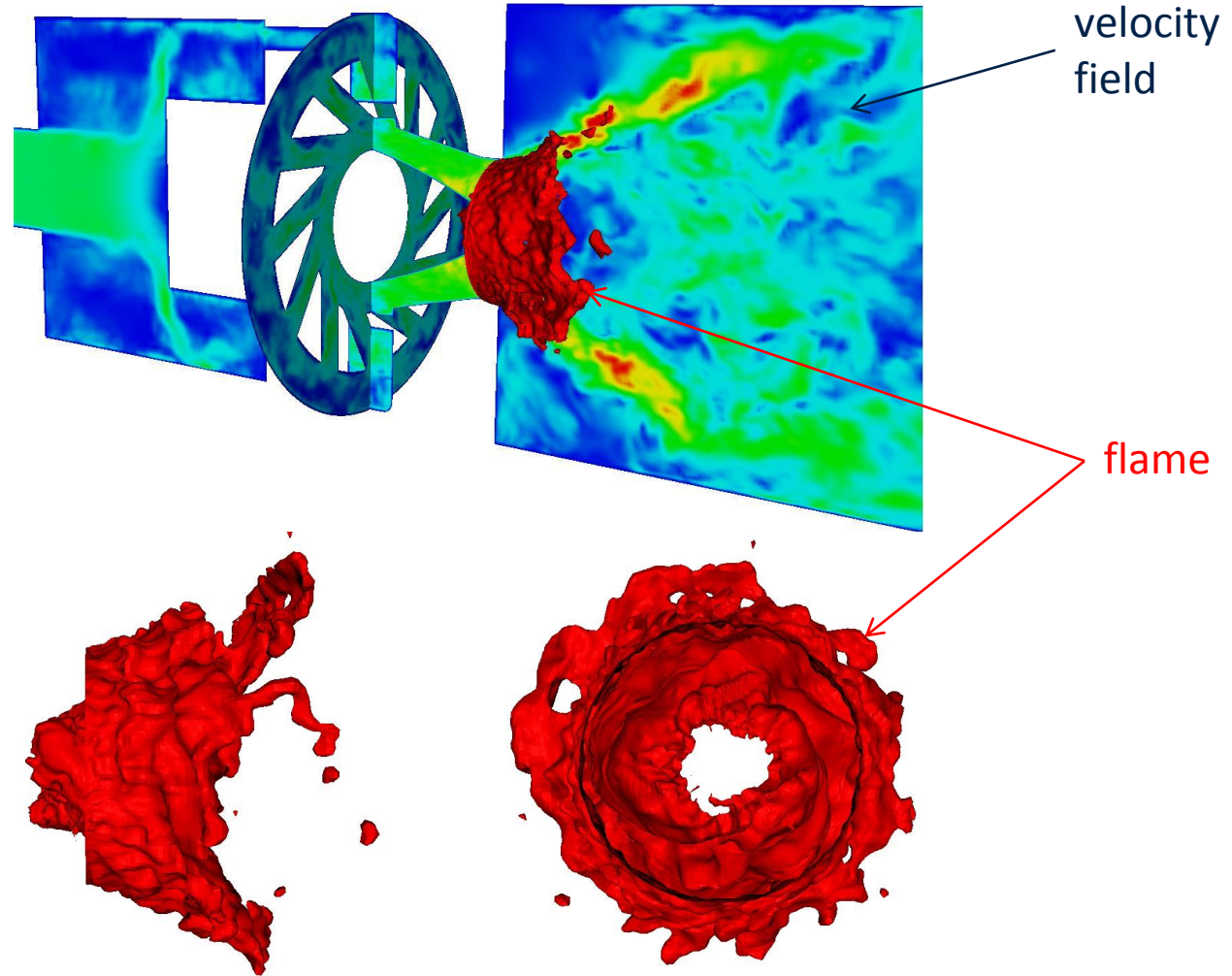
2014

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Example: LES of a stationary gas turbine



Part II: Turbulent Combustion

- Turbulence
 - **Turbulent Premixed Combustion** 
 - Turbulent Non-Premixed Combustion
 - Modelling Turbulent Combustion
 - Applications
- **Scales of Turbulent Premixed Combustion**
 - Regime-Diagram
 - Turbulent Burning Velocity

Scales of Turbulent Premixed Combustion

- Integral turbulent scales

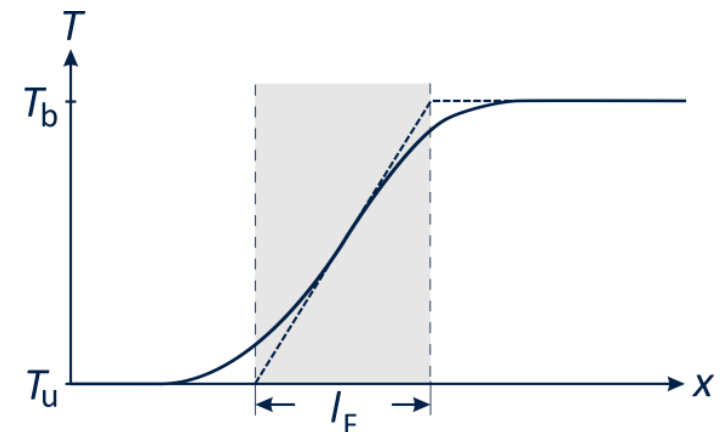
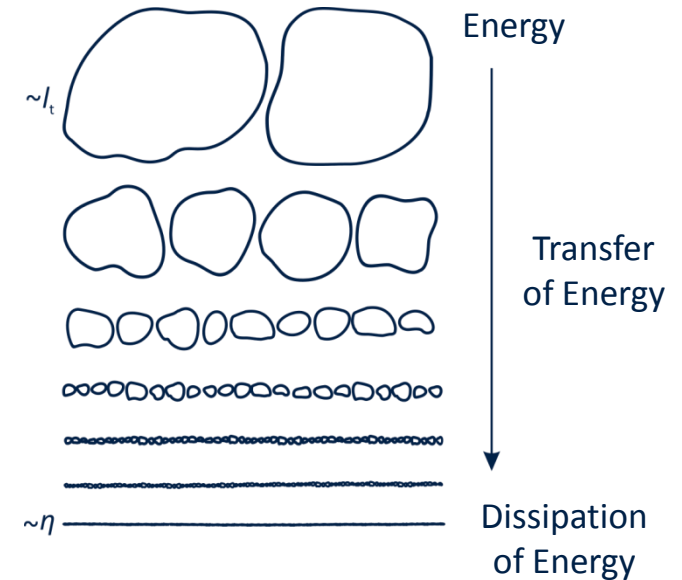
$$l_t = c_1 \frac{\bar{k}^{3/2}}{\bar{\varepsilon}}, \quad u' = \sqrt{\frac{2}{3} \bar{k}}, \quad \tau = \frac{l_t}{u'} \sim \frac{\bar{k}}{\bar{\varepsilon}}$$

- Smallest turbulent scales/Kolmogorov scales

$$\eta = \left(\frac{\nu^3}{\bar{\varepsilon}} \right)^{1/4}, \quad u_\eta = (\nu \bar{\varepsilon})^{1/4}, \quad t_\eta = \left(\frac{\nu}{\bar{\varepsilon}} \right)^{1/2}$$

- Flame thickness and time, reaction zone thickness

$$l_F = \frac{D}{s_L} = \frac{\lambda_b}{\rho_u c_p s_L}, \quad t_F = \frac{l_F}{s_L} = \frac{D}{s_L^2}, \quad l_\delta \ll l_F$$



Dimensionless Quantities in Premixed Turbulent Combustion

- Turbulent Reynolds number

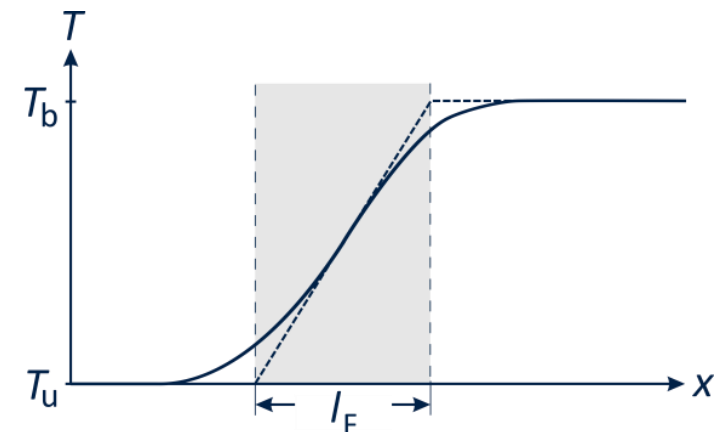
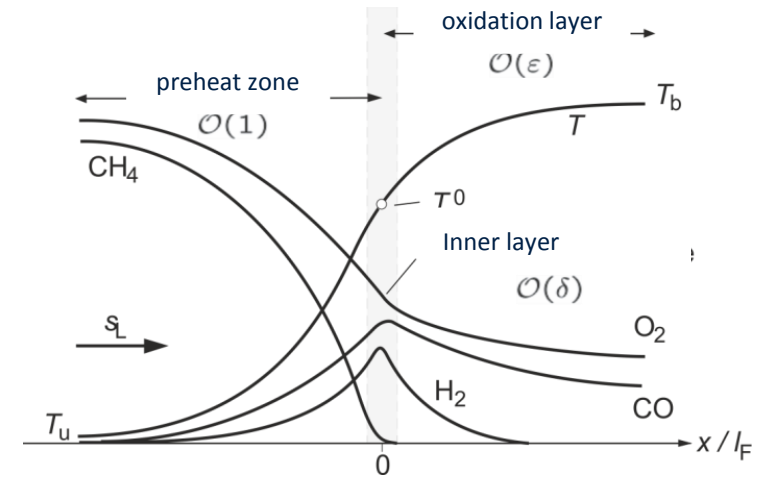
$$Sc = \frac{\nu}{D} = 1 \quad \rightarrow \quad Re_t = \frac{l_t u'}{l_F s_L}$$

- Turbulent Damköhler number

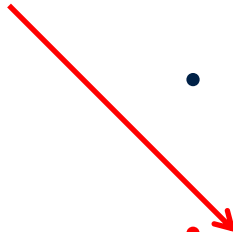
$$Da_t = \frac{\tau}{t_F} = \frac{l_t s_L}{l_F u'}$$

- Karlovitz number** (interaction of small-scale turbulence with the flame)

$$Ka = \frac{t_F}{t_\eta} = \frac{l_F^2}{\eta^2} = \sqrt{\frac{l_F}{l_t} \left(\frac{u'}{s_L} \right)^3} \quad \text{und} \quad Ka_\delta = \frac{l_\delta^2}{\eta^2} = \overset{\delta \approx 0,1}{\delta^2} Ka$$



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 - Turbulent Burning Velocity
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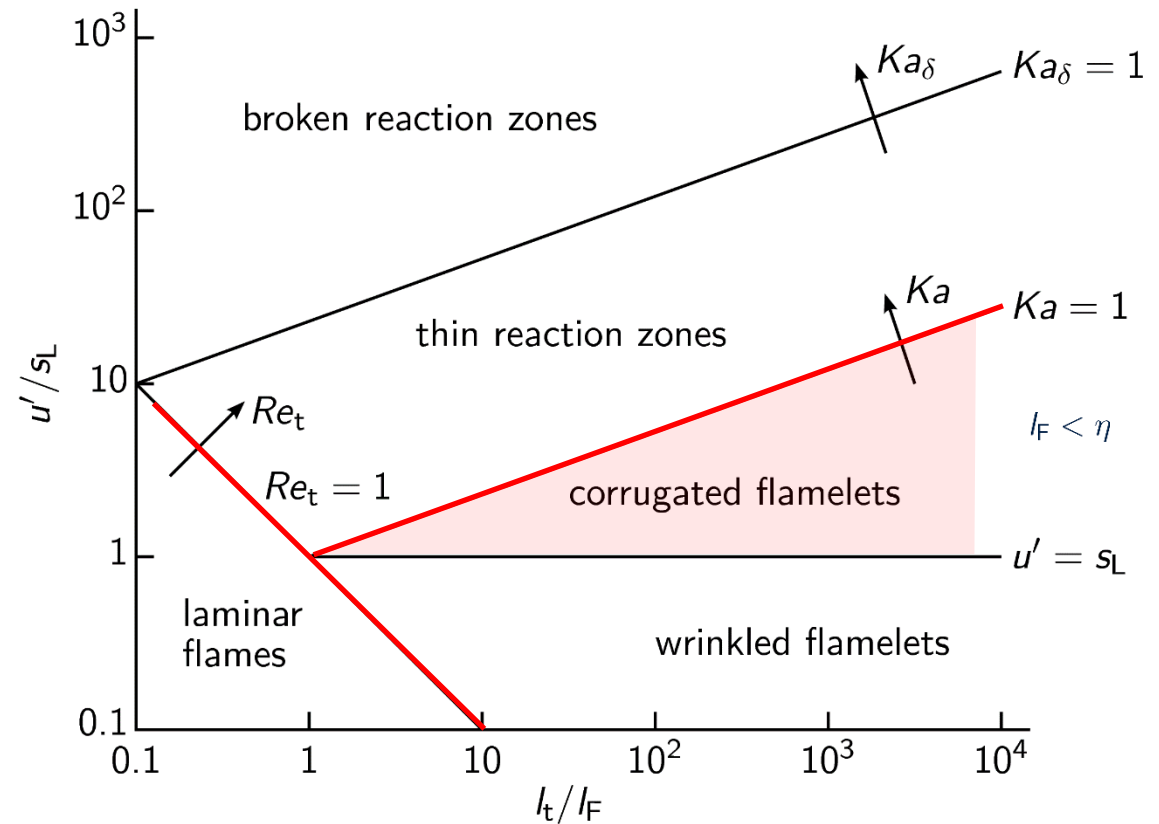
Regime Diagram

Corrugated Flamelet Regime

$$Re_t = \frac{l_t u'}{l_F s_L}$$

$$Ka^2 = \left(\frac{l_t}{l_F}\right)^{-1} \left(\frac{u'}{s_L}\right)^3$$

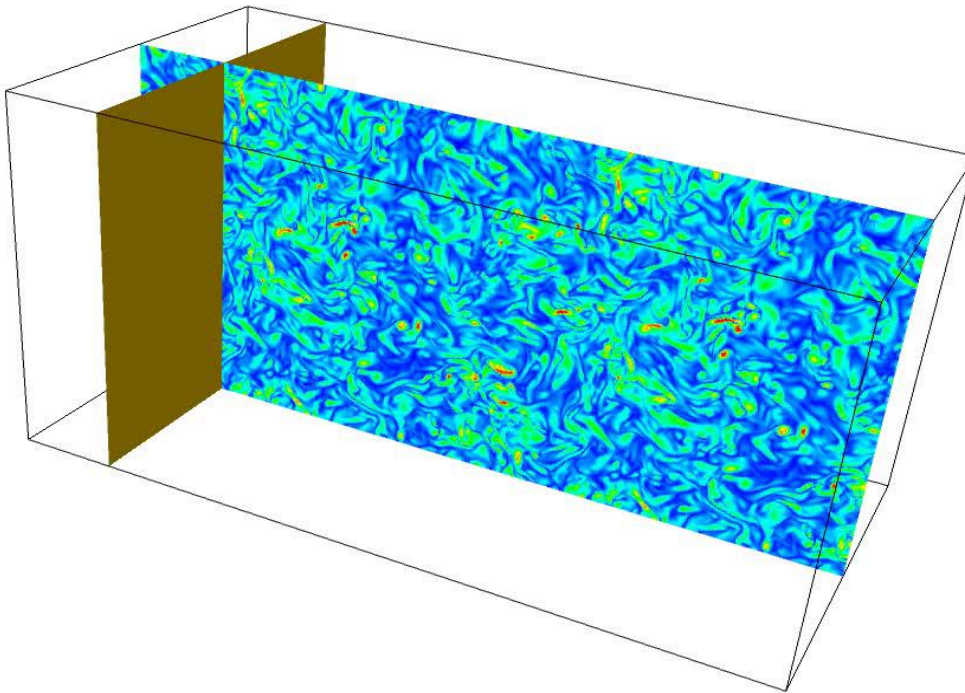
$$Da_t = \frac{l_t}{l_F} \left(\frac{u'}{s_L}\right)^{-1}$$



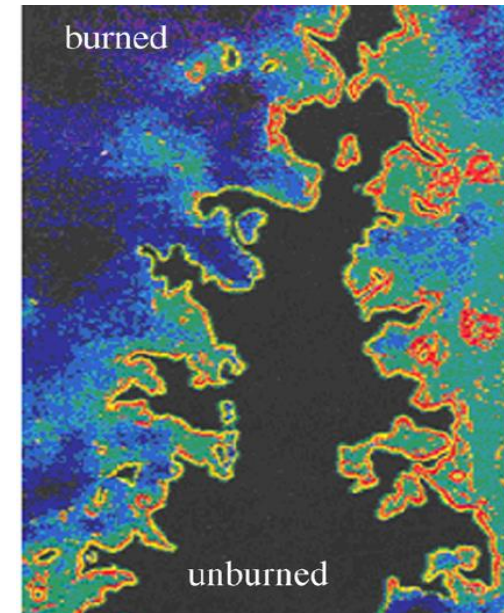
Regime Diagram: Corrugated Flamelets

- $Ka < 1 \rightarrow \eta > l_F$
 - Interaction of a very **thin flame** with a turbulent flow
 - Assumption: **infinitely thin flame** (compared to turbulent scales)

premixed flame in isotropic turbulence



OH-radical-distribution in a turbulent premixed flame



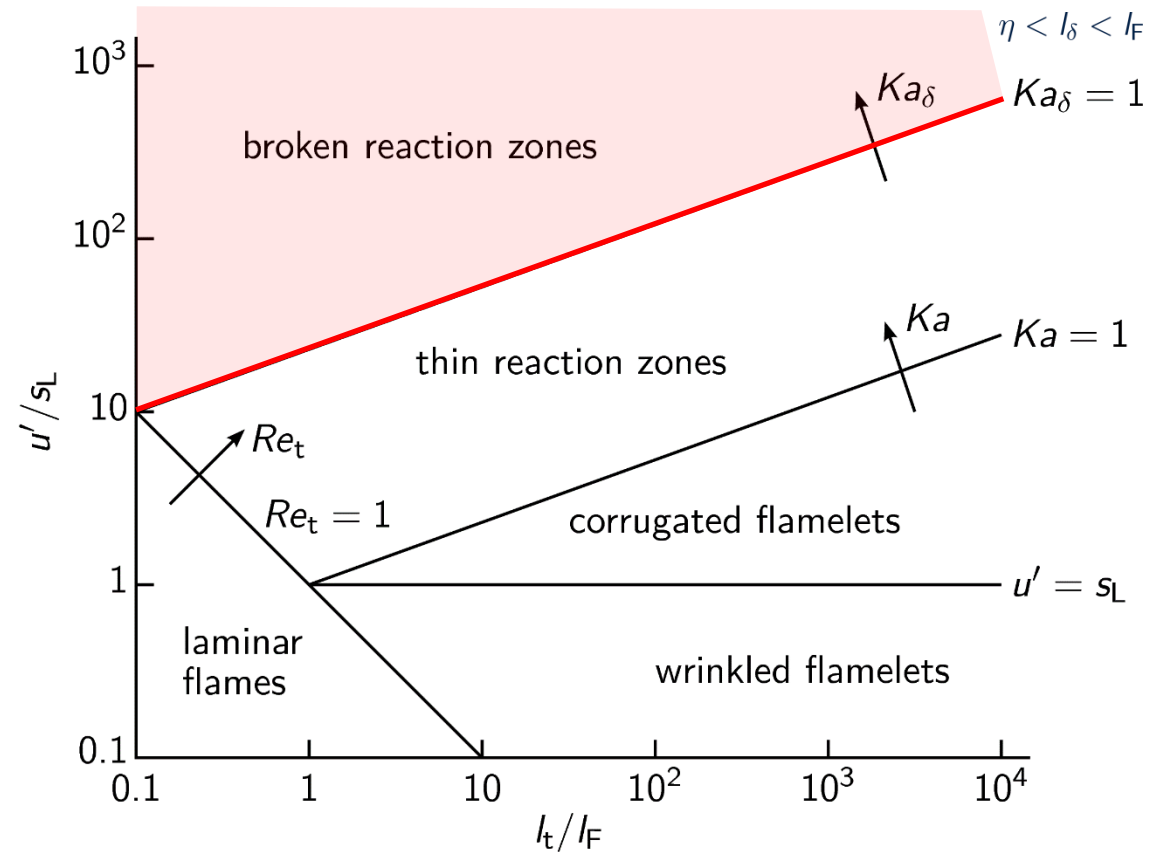
Buschmann (1996)

Regime Diagramm: Broken Reaction Zones Regime

$$Re_t = \frac{l_t u'}{l_F s_L}$$

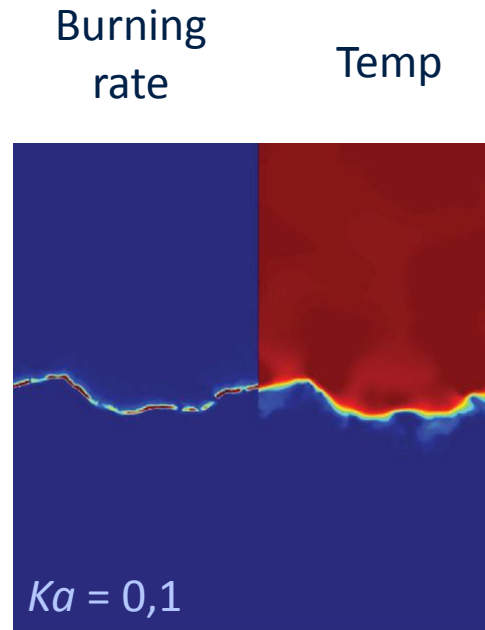
$$Ka^2 = \left(\frac{l_t}{l_F}\right)^{-1} \left(\frac{u'}{s_L}\right)^3$$

$$Da_t = \frac{l_t}{l_F} \left(\frac{u'}{s_L}\right)^{-1}$$

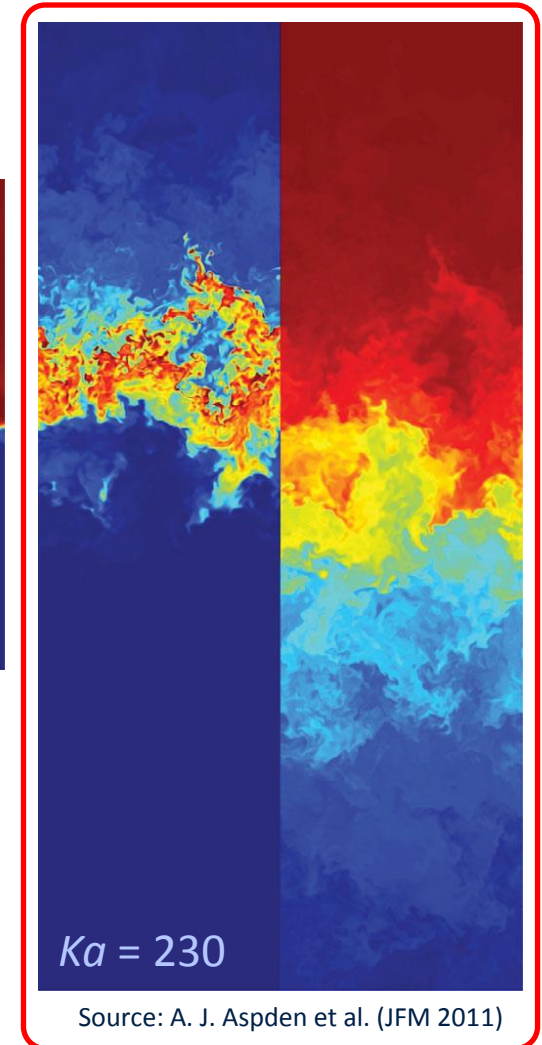


Regime Diagram: Broken Reaction Zones Regime

- $Ka_\delta > 1 \rightarrow \eta < l_\delta$
 - Smallest **turbulent eddies** enter **the reaction zones**
 - Turbulent transport \rightarrow **radicals** are removed **from reaction zone**
 - Local **extinguishing** in the inner reaction zone
 - Overall extinguishing of the flame front is possible



Two-dimensional slices from three-dimensional simulations of low- and high-Karlovitz-supernovae flames, respectively. The left-hand panel in each case is burning rate, and the right-hand panel is temperature.



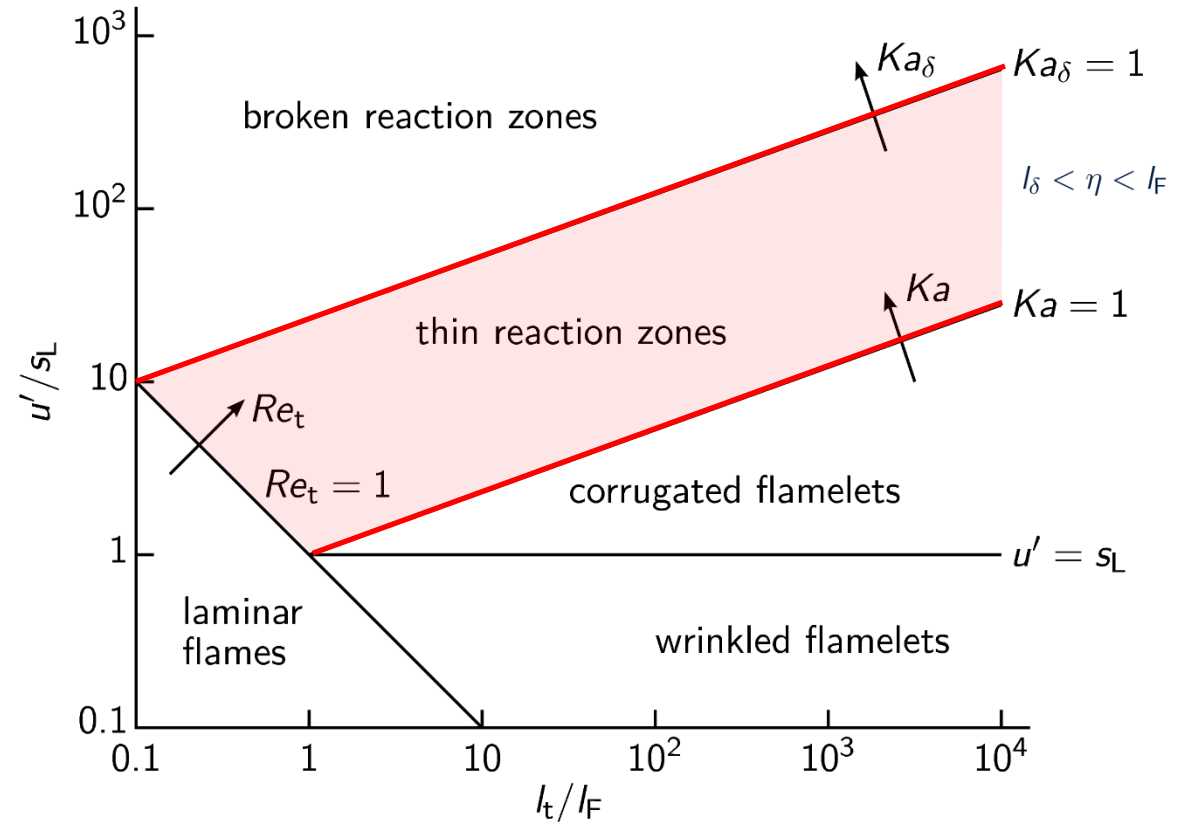
Source: A. J. Aspden et al. (JFM 2011)

Regime Diagramm: Thin Reaction Zones Regime

$$Re_t = \frac{l_t u'}{l_F s_L}$$

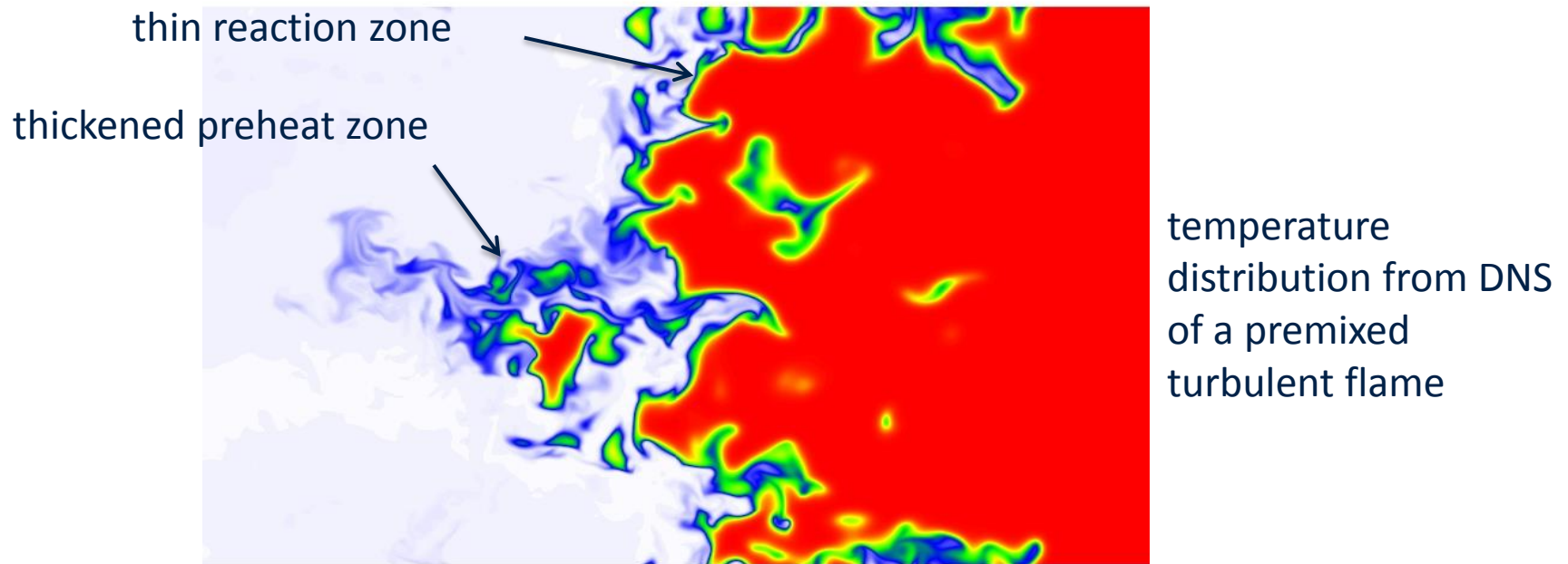
$$Ka^2 = \left(\frac{l_t}{l_F}\right)^{-1} \left(\frac{u'}{s_L}\right)^3$$

$$Da_t = \frac{l_t}{l_F} \left(\frac{u'}{s_L}\right)^{-1}$$



Regime Diagramm: Thin Reaction Zones Regime

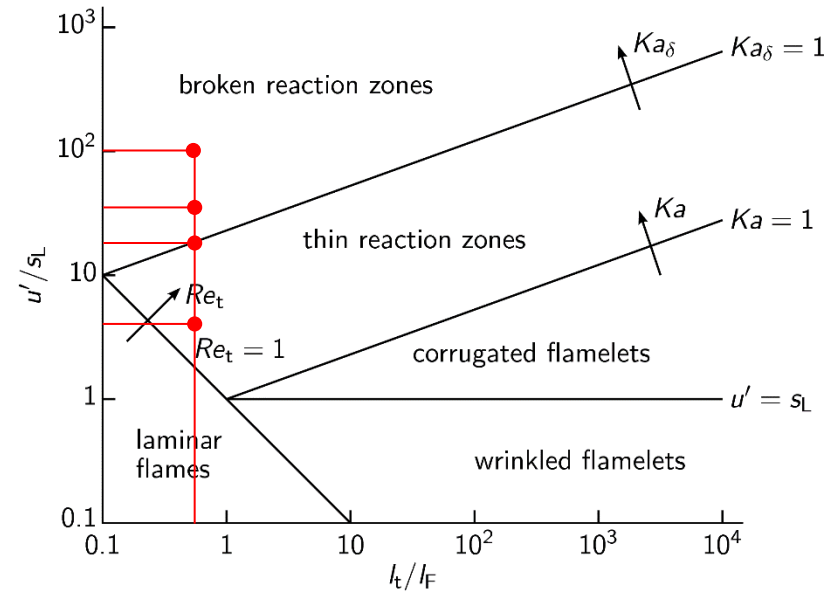
- $Ka > 1$ und $Ka_\delta < 1 \rightarrow l_\delta < \eta < l_F$
 - With $l_\delta \approx 0,1l_F \rightarrow Ka \approx 100Ka_\delta$
 - Turbulent mixing inside preheat zone
 - Assumption: **infinitely thin reaction zone** (compared to turbulent scales)



Regime Diagram: Résumé

Case	A40	B40	C40	D40
Equivalence ratio (φ)	0.40	0.40	0.40	0.40
→ Flame speed (s_L) (m s^{-1})	2.24×10^{-1}	2.24×10^{-1}	2.24×10^{-1}	2.24×10^{-1}
→ Flame width (l_L) (m)	6.29×10^{-4}	6.29×10^{-4}	6.29×10^{-4}	6.29×10^{-4}
Domain width (L) (m)	3.14×10^{-3}	3.14×10^{-3}	3.14×10^{-3}	3.14×10^{-3}
Domain height (H) (m)	2.512×10^{-2}	2.512×10^{-2}	2.512×10^{-2}	2.512×10^{-2}
→ Integral length scale (l) (m)	3.14×10^{-4}	3.14×10^{-4}	3.14×10^{-4}	3.14×10^{-4}
Length ratio (l/l_L)	0.5	0.5	0.5	0.5
→ RMS velocity (\ddot{u}) (m s^{-1})	0.825	3.83	7.34	23.9
Velocity ratio (\ddot{u}/s_L)	3.69	17.1	32.9	106.8
Karlovitz number (Ka_L)	10	100	266	1562
Damköhler number (Da_L)	1.36×10^{-1}	2.92×10^{-2}	1.52×10^{-2}	4.68×10^{-3}
Levels of refinement	1	1	1	2
Effective resolution (N)	$128^2 \times 1024$	$128^2 \times 1024$	$128^2 \times 1024$	$256^2 \times 2048$
Cell width (Δx) (m)	2.45×10^{-5}	2.45×10^{-5}	2.45×10^{-5}	1.23×10^{-5}
Kolmogorov length (η) (m)	4.33×10^{-5}	1.37×10^{-5}	8.41×10^{-6}	3.47×10^{-6}
Cell Kolmogorov length ($\eta_{\Delta x}$) (m)	7.36×10^{-6}	7.36×10^{-6}	7.36×10^{-6}	3.68×10^{-6}
Effective Kolmogorov length (η_e) (m)	4.33×10^{-5}	1.51×10^{-5}	11.2×10^{-6}	5.12×10^{-6}

TABLE 2. Turbulent flame properties for the four simulations at equivalence ratio $\varphi = 0.40$.



Source: A. J. Aspden et al. (JFM 2011)

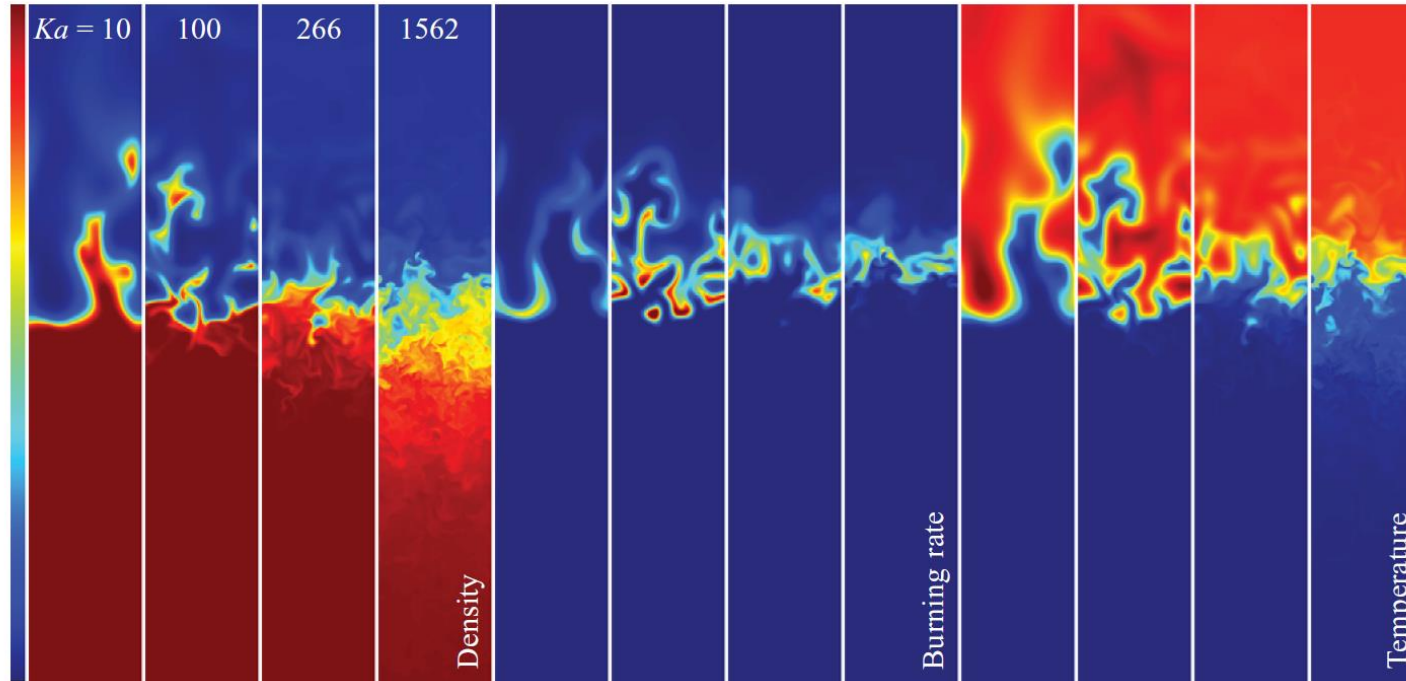
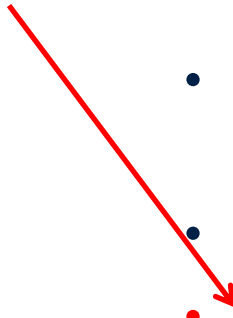


FIGURE 8. Two-dimensional vertical slices through three-dimensional simulations showing density, burning rate and temperature at $\varphi = 0.40$, respectively. The density, burning rate and temperature ranges are $[0.2, 1.02] \text{ kg m}^{-3}$, $[0, 64] \text{ kg m}^{-3} \text{ s}^{-1}$ and $[298, 1600] \text{ K}$, respectively.

Source: A. J. Aspden et al. (JFM 2011)

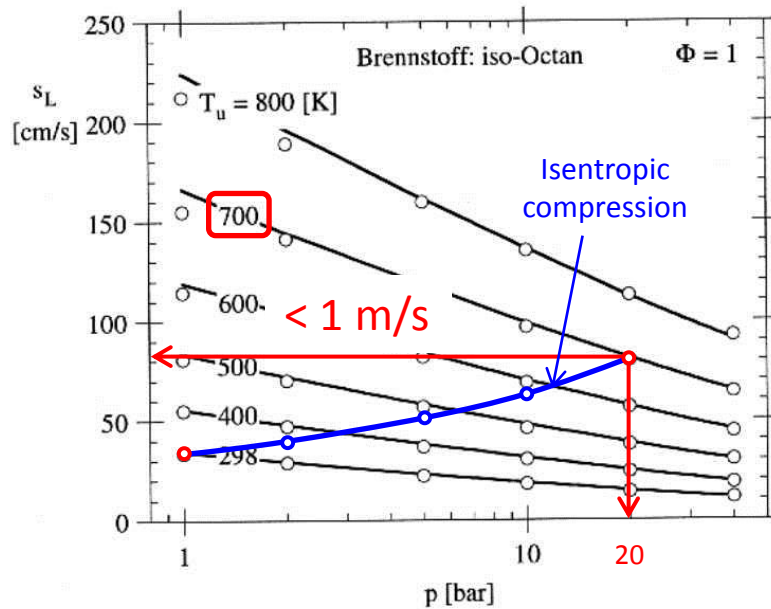
Course Overview

Part II: Turbulent Combustion

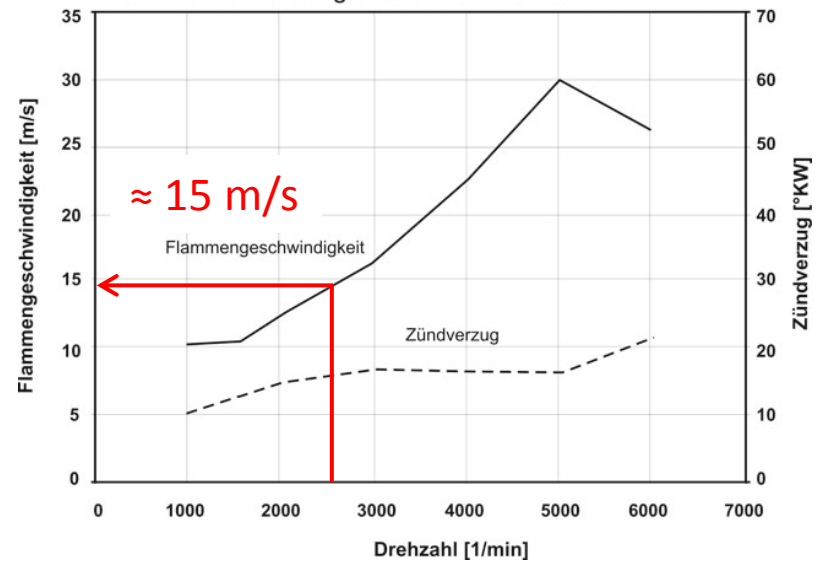
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- 

Turbulent Burning Velocity

Comparison: Laminar/Measured Burning Velocity

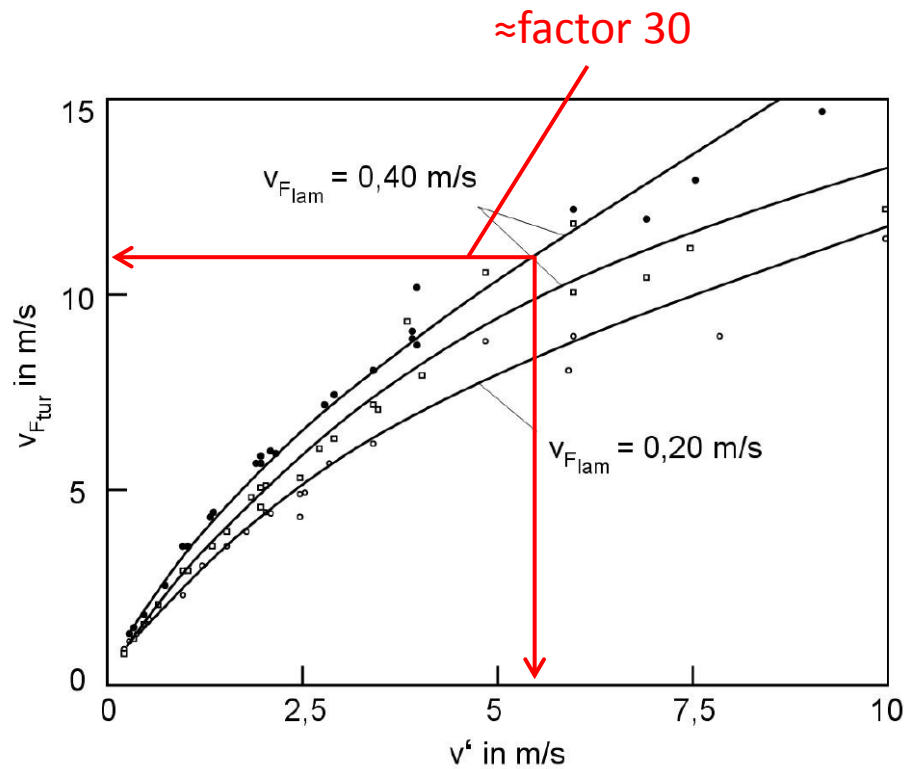


Laminar burning velocity of iso-octane



Exemplary measurements in gasoline engine with tumble generator of flame velocity at spark plug position during full load (Source: Merker, „Grundlagen Verbrennungsmotoren“)

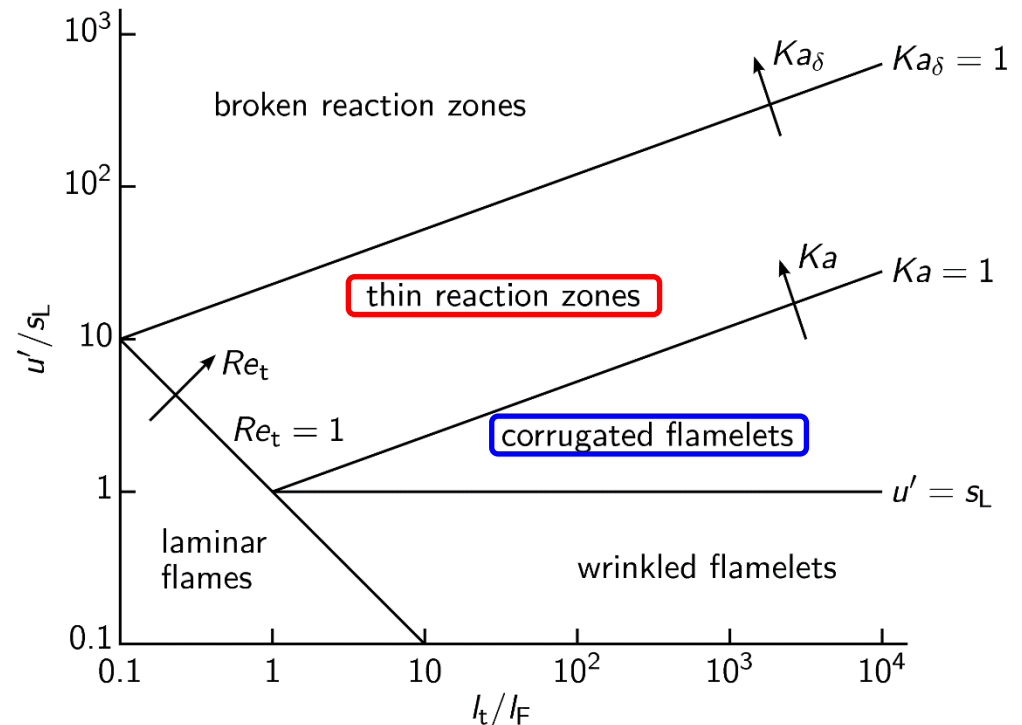
Comparison: Laminar/Measured Burning Velocity



Experimental data of s_T vs. wrinkled laminar-flame theories of turbulent flame propagation (data from Turns 2000)

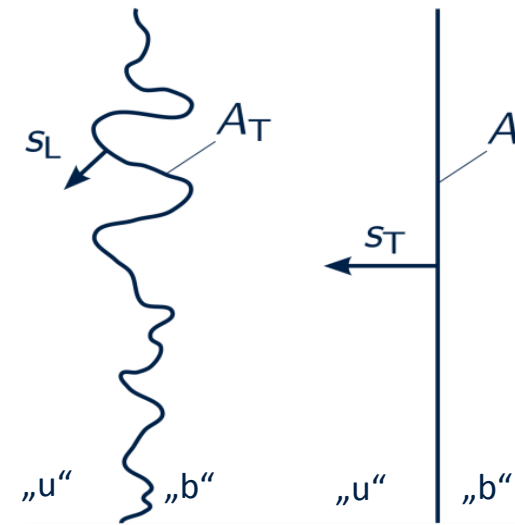
Turbulent Burning Velocity

- Main problem for turbulent premixed combustion:
Quantification of turbulent burning velocity s_T
- s_T : Velocity which quantifies the propagation of the **turbulent flame front into unburnt mixture**
- Distinction of two limiting cases by Damköhler (1940)
 1. Large scale turbulence \leftrightarrow **corrugated flamelets**
 2. Small scale turbulence \leftrightarrow **thin reaction zones**



Turbulent Burning Velocity: Corrugated Flamelets

- Instantaneous flame front
 - Flame surface area A_T
 - Propagates locally with **laminar burning velocity** s_L into unburnt mixture
- Mean flame front
 - Mean flame surface area A
 - Propagates with **turbulent burning velocity** s_T



Turbulent Burning Velocity: Corrugated Flamelets

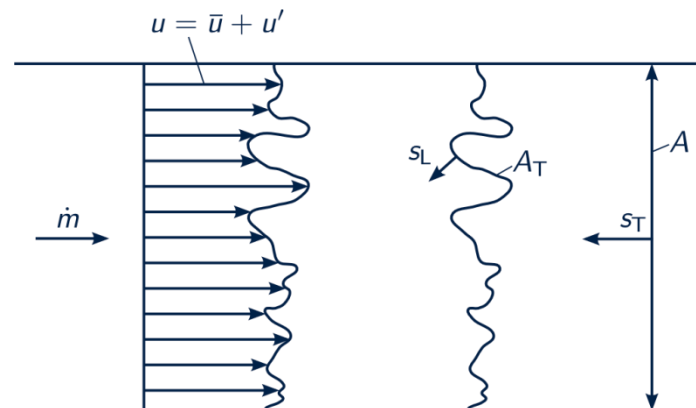
- With the **mass flux** through A and A_T

$$\dot{m} = \rho_u s_L A_T = \bar{\rho}_u s_T A$$

- Assume constant density in the unburnt mixture (assumption) ($\rho_u = \bar{\rho}_u$)

$$\frac{s_T}{s_L} = \frac{A_T}{A}$$

- Wrinkling of the laminar flame ($A_T \uparrow$) \rightarrow increase of s_T



Turbulent Burning Velocity: Corrugated Flamelets

- Turbulence \rightarrow flame surface area \uparrow
- Using an analogy with a Bunsen flame

$$s_L = u_u \sin \alpha \xrightarrow{\text{hier}} \sin \alpha = \frac{s_L}{u'} \Rightarrow \frac{A_T}{A} \sim \frac{d / \sin \alpha}{d} = \frac{u'}{s_L}$$

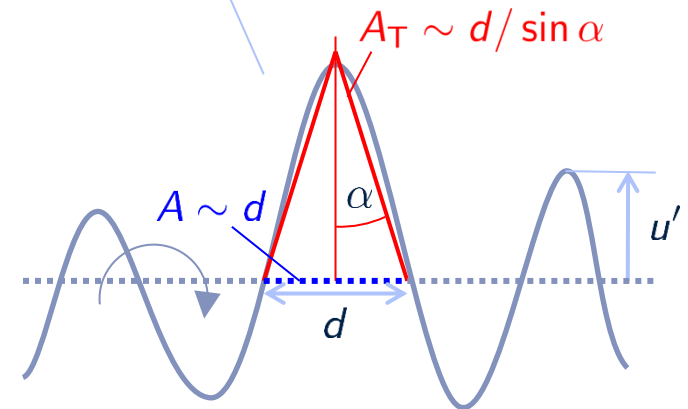
- Limit for $u' \rightarrow 0$

$$\frac{s_T}{s_L} = \frac{A_T}{A} = 1 + \frac{u'}{s_L}$$

- Internal combustion engine:
 - Engine speed $n \uparrow \rightarrow$ burning velocity $s_T \uparrow$ due to

$$u' \sim u_{\text{piston}} \sim n$$

\rightarrow High engine speed achievable

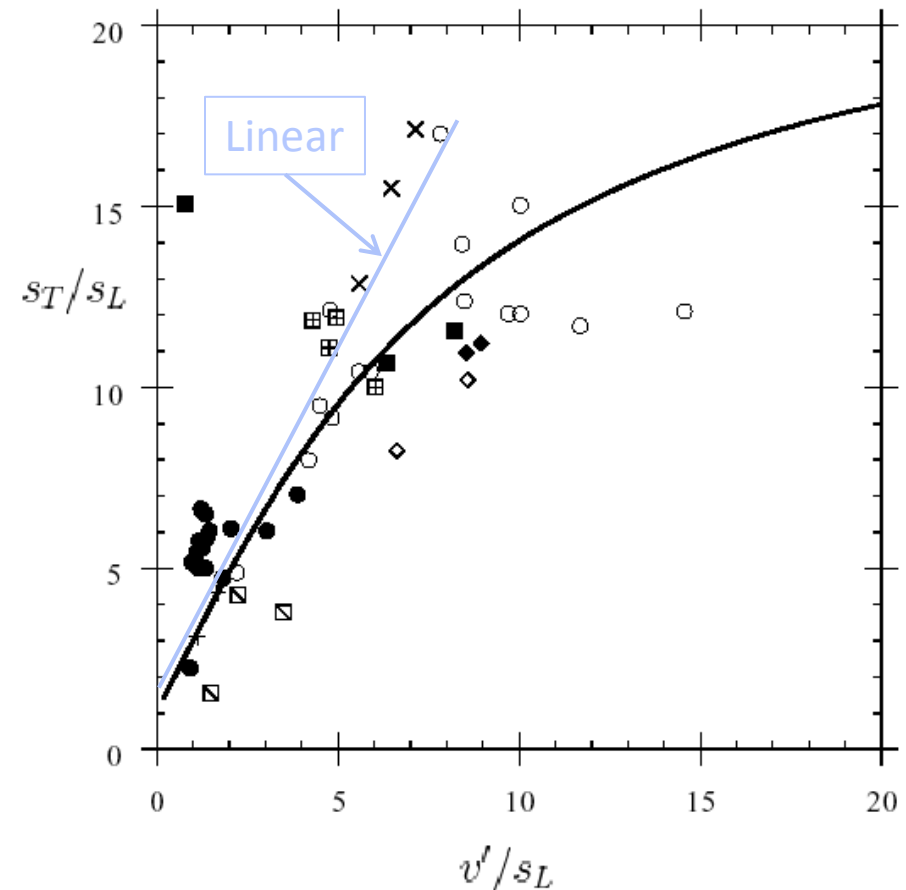


Turbulent Burning Velocity: large-scale turbulence

- In experiments often used empirical relation

$$\frac{s_T}{s_L} = 1 + C \left(\frac{u'}{s_L} \right)^n$$

- Constant C experimentally determined
- Typical values: $0.5 < n < 1.0$
- From experimental data →
 - For small u' , $s_T \sim u'$ applies
 - Consistent with Damköhler theory
 - Increase of turbulent intensity
 - s_T grows linearly
 - With further increase less than linear



Turbulent Burning Velocity: **Thin Reaction Zones**

- Reduced increase of turbulent burning velocity
 → second limiting case of Damköhler
- **Thin reaction zones**/small-scaled turbulence
- In analogy to

Damköhler uses

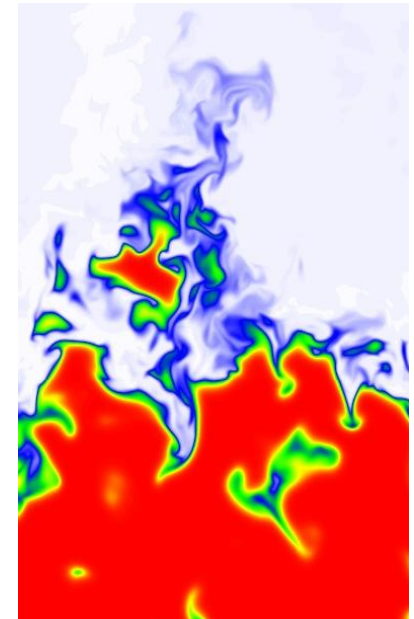
$$s_L = \sqrt{\frac{D}{t_c}}$$

$$s_T = \sqrt{\frac{D_t}{t_c}}$$

$$\frac{s_T}{s_L} = \sqrt{\frac{D_t}{D}} = \sqrt{\frac{0,78u'l_t}{s_L l_F}}$$

$$s_T \sim \sqrt{u'l_t}$$

consistent with experimental data



Turbulent Burning Velocity

- Damköhler-limits can be combined to a single formula (Peters, 1999):

$$\frac{s_T}{s_L} = 1 - \alpha \frac{l_t}{l_F} + \sqrt{\left(\alpha \frac{l_t}{l_F}\right)^2 + 4\alpha \frac{u' l_t}{s_L l_F}}$$

– constant $\alpha = 0,195$

- Low turbulence intensity →

$$\frac{s_T}{s_L} = 1 + 2 \frac{u'}{s_L}$$

- High turbulence intensity →

$$\frac{s_T}{s_L} = 1 + \sqrt{\frac{0,78 u' l_t}{s_L l_F}}$$

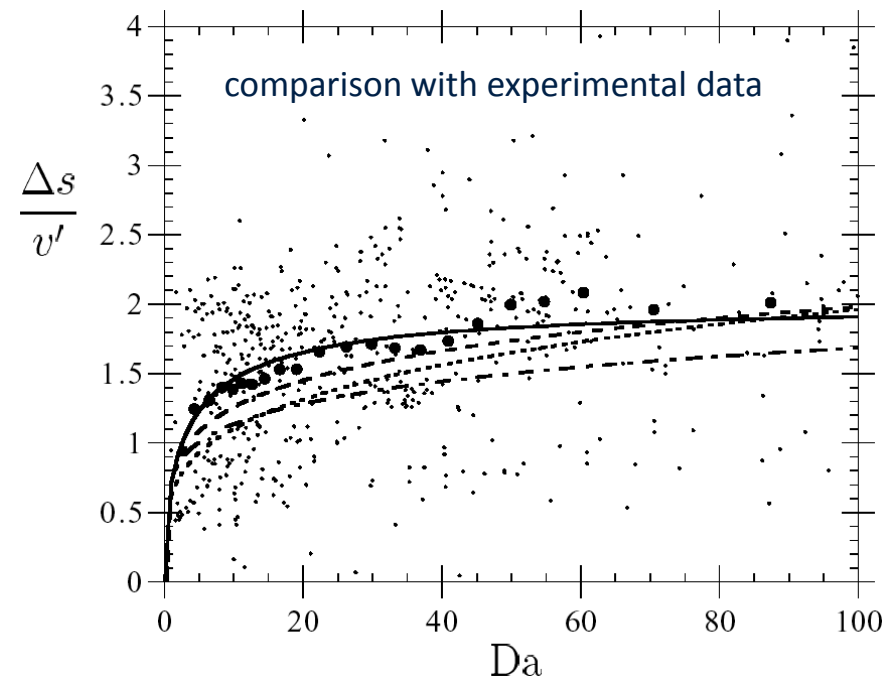
Turbulent Burning Velocity

- By rearranging this formula with $Da_t = (l_t s_L)/(l_F u')$ →

$$\frac{s_T - s_L}{u'} = -\alpha Da_t + \sqrt{\alpha^2 Da_t^2 + 4\alpha Da_t}$$

- Limit for high Damköhler number →

$$\lim_{Da_t \rightarrow \infty} \frac{s_T - s_L}{u'} = 2$$



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